

Experimental Status of the CKM angle β



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(For the *BABAR* Collaboration)

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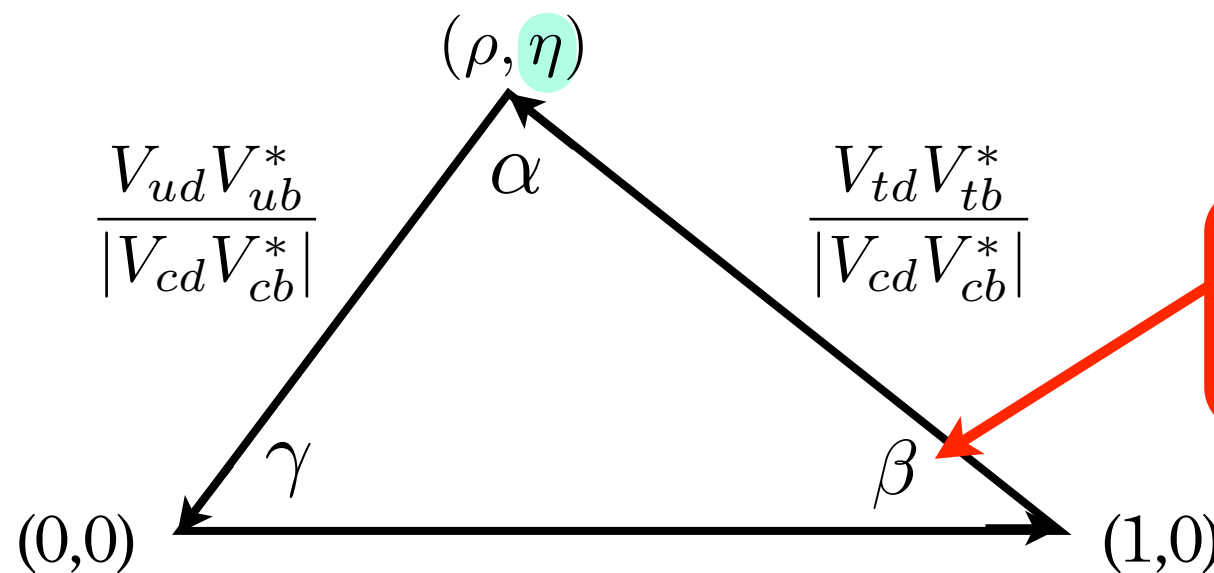
CP violation in Standard Model

- Arises from single phase in CKM matrix:

$$V_{\text{CKM}} = \begin{bmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{bmatrix} \simeq \begin{bmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{bmatrix}$$

$$\lambda \equiv \sin \theta_{\text{Cabibbo}}$$

- Unitarity of V_{CKM} can be represented as a triangle in the complex plane:

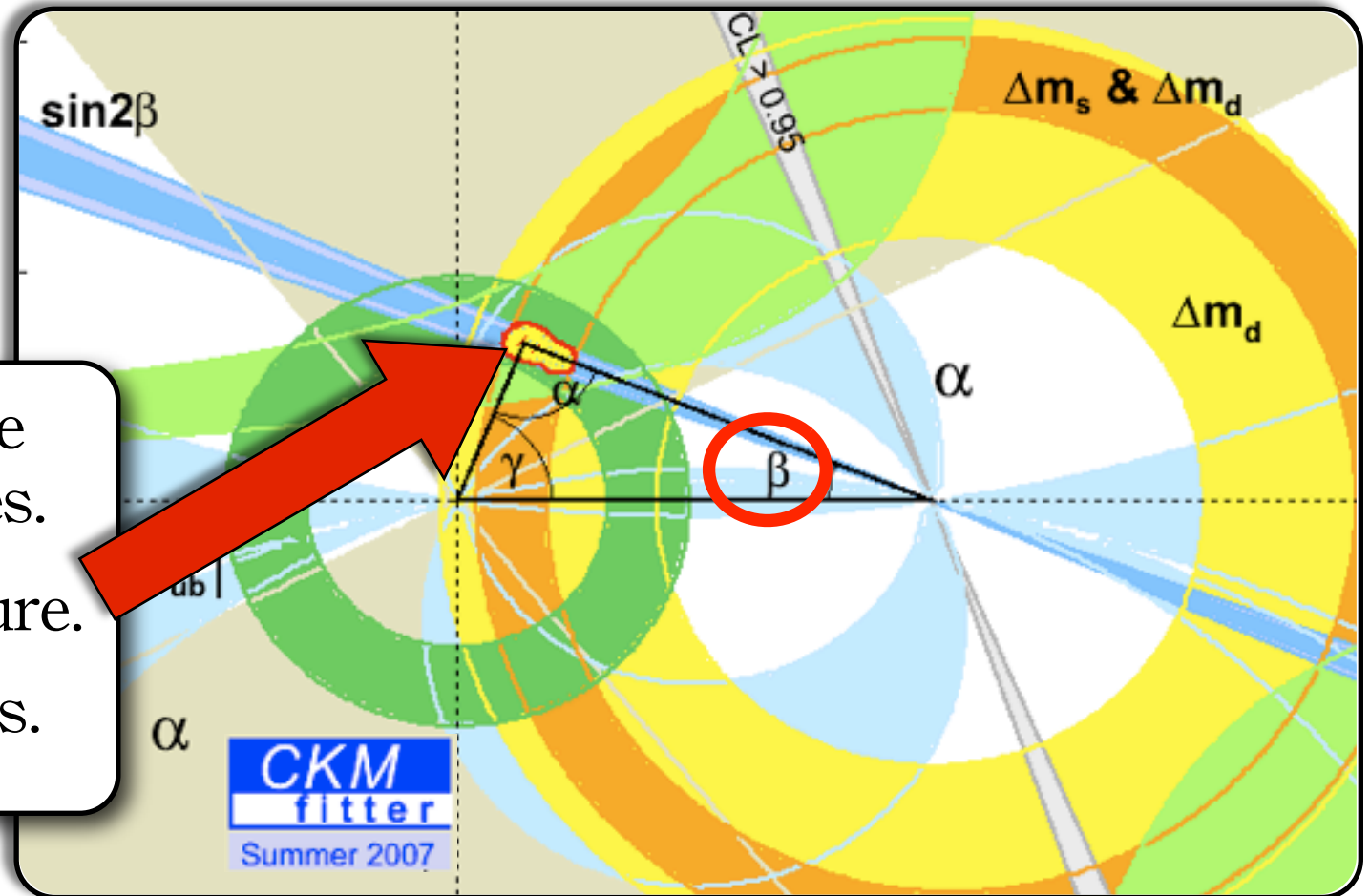


$$\beta \equiv \arg \left[-\frac{V_{cd} V_{cb}^*}{V_{td} V_{tb}^*} \right]$$

$$(\beta, \alpha, \gamma) = (\phi_1, \phi_2, \phi_3)$$

Overconstraining the triangle

- Measure the sides and angles of the unitary triangle in diverse processes.
- Agreement confirms the CKM picture.
- Disagreement indicates new physics.



Wassili Kandinsky
Composition VIII, 1923

Mixing-induced CP violation

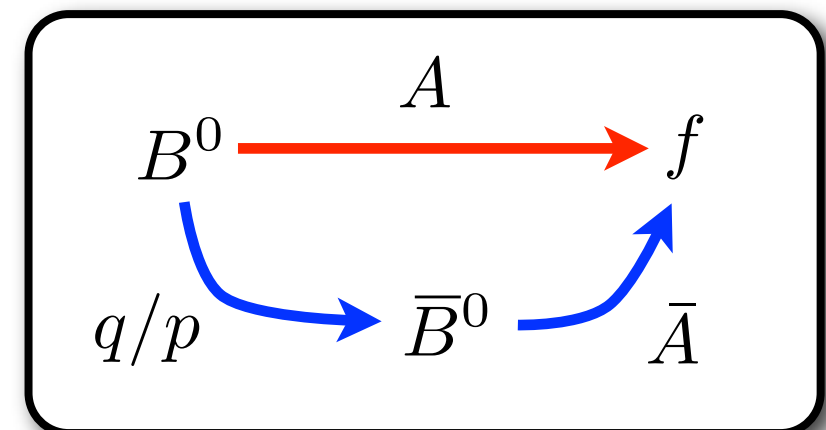
- For B meson pairs, produced coherently in $\Upsilon(4S) \rightarrow B^0 \bar{B}^0$, time dependent decay rate asymmetry (to CP eigenstate f):

$$A_f(t) = \frac{\Gamma(\bar{B}^0(t) \rightarrow f) - \Gamma(B^0(t) \rightarrow f)}{\Gamma(\bar{B}^0(t) \rightarrow f) + \Gamma(B^0(t) \rightarrow f)} = -S_f \sin(\Delta m_B t) + C_f \cos(\Delta m_B t)$$

- Final state f is reached from B^0 and \bar{B}^0 , so amplitudes for **decay** and **mixing+decay** interfere:
- We define S_f and C_f in terms of λ_f :

$$S_f \equiv \frac{-2\text{Im}\lambda_f}{1 + |\lambda_f|^2} \quad C_f \equiv \frac{1 - |\lambda_f|^2}{1 + |\lambda_f|^2}$$

- Interference causes $\text{Im } \lambda_f \neq 0$, though $|\lambda_f| = 1$.



$$\lambda_f \equiv \eta_f \frac{q}{p} \frac{\bar{A}_f}{A_f}$$

← ratio of decay amplitudes

↑ CP eigenvalue

← mixing amplitude

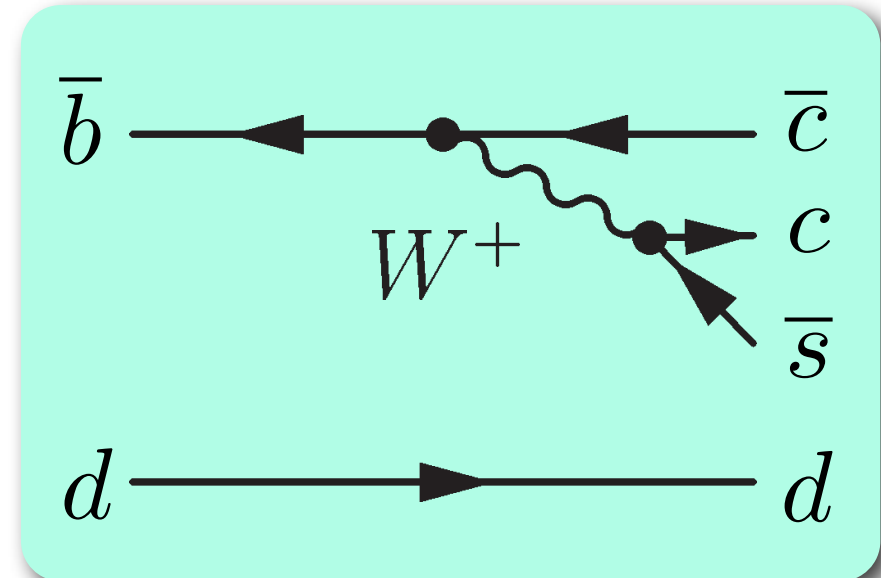
$$S_{c\bar{c}s} = \sin 2\beta$$

- Tree dominated $b \rightarrow c\bar{c}s$ decays.

- $B^0 \rightarrow J/\psi K_S^0$
- $B^0 \rightarrow J/\psi K_L^0$,
- $B^0 \rightarrow \psi(2S)K_S^0$,
- $B^0 \rightarrow J/\psi K^{*0}$ etc.

- Theoretically very clean, in SM:

$$\begin{aligned} S &= \sin 2\beta \\ C &= 0 \end{aligned}$$



“Golden mode” :

- large branching fraction ($\sim 10^{-3}$).
- good reconstruction efficiency (30%).
- experimentally clean signature.

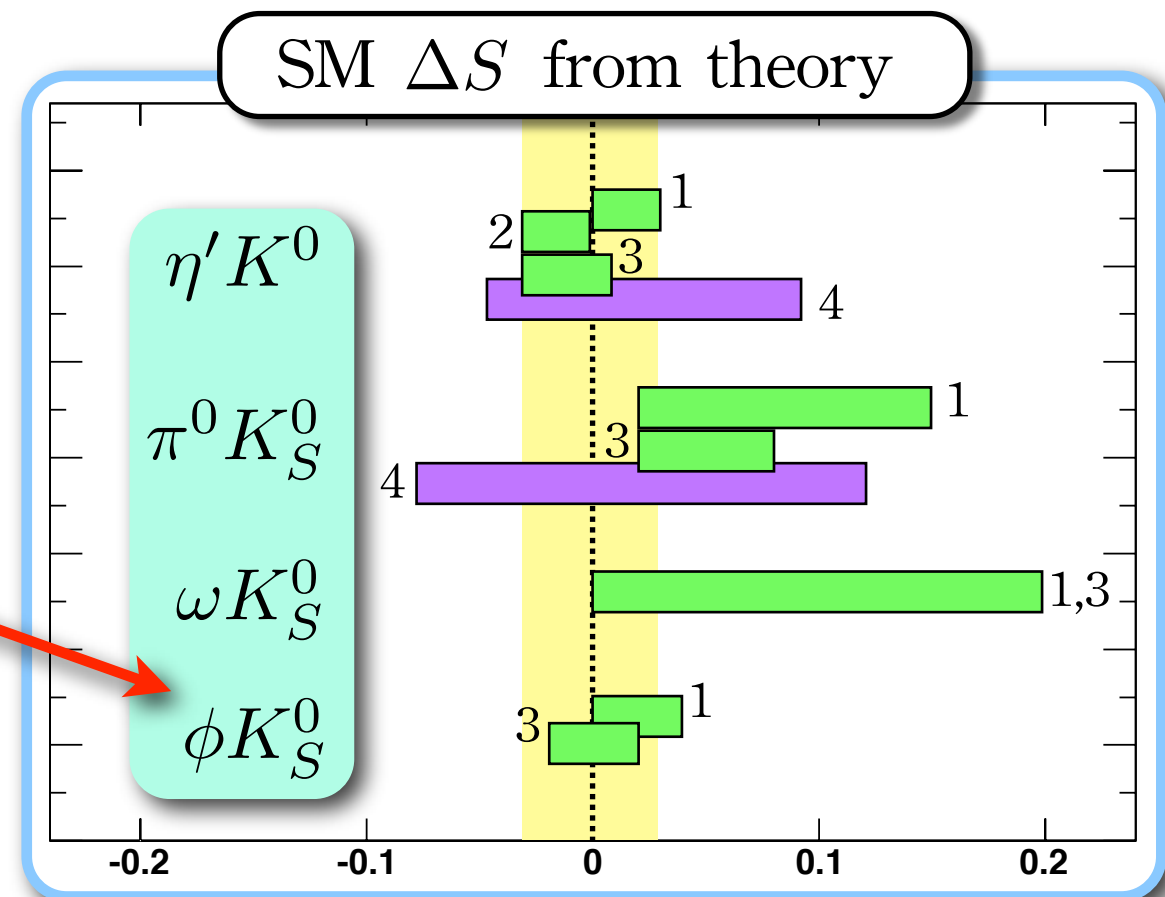
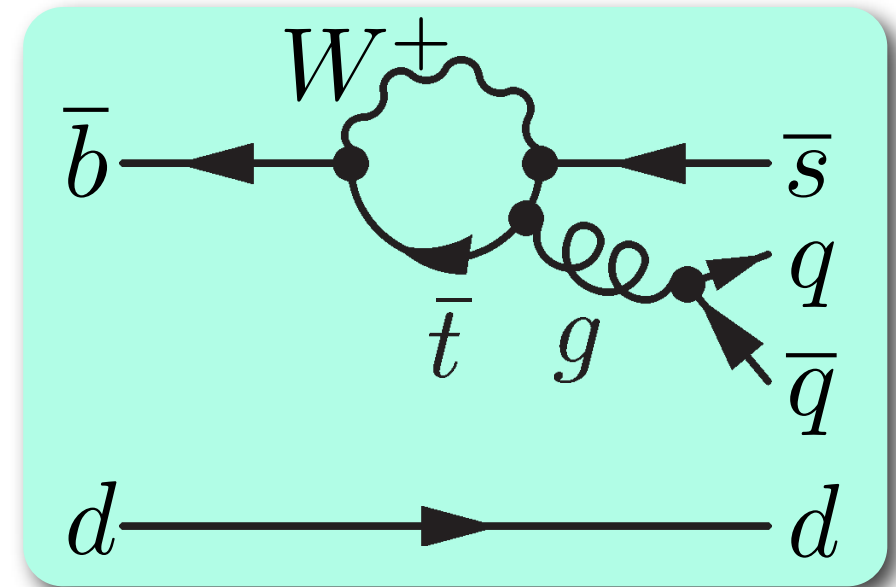
$$S_f = \sin 2\beta_{\text{eff}}$$

- Penguin dominated $b \rightarrow q\bar{q}s$ decays.
 - $B^0 \rightarrow \eta' K^0, \phi K^0$, etc.
- Pollution from secondary amplitudes:

$$\begin{aligned} S_f &\simeq \sin 2\beta \equiv \sin 2\beta_{\text{eff}} \\ C_f &\simeq 0 \end{aligned}$$

- In clean modes, SM suggests

$$\Delta S \equiv \sin 2\beta_{\text{eff}} - \sin 2\beta \simeq 0.03$$
- Sensitive to new particles in loop.
- Large ΔS indicates new physics.



¹QCDF Beneke, PLB620, 143 (2005)

²SCET/QCDF Williamson, Zupan, PRD74, 014003 (2006)

³QCDF Cheng, Chua, Soni, PRD72, 014006 (2005)

⁴SU(3) Gronau, Rosner, Zupan, PRD74, 093003 (2006)

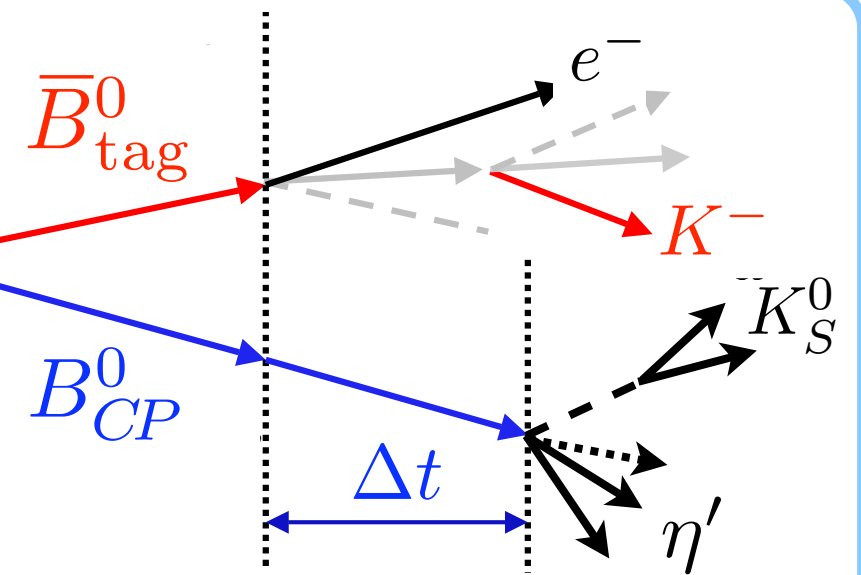
Time dependent analysis

- Fully reconstruct B_{CP} ; partially reconstruct B_{tag} .
 - Measure Δz , convert to Δt .
 - Determine flavor of B_{tag} .

$$\Upsilon(4S) \rightarrow$$

$$\Delta z = \beta \gamma c \Delta t$$

$$\Delta t = t_{CP} - t_{\text{tag}}$$



Effective tagging efficiency:

$$Q = (31.2 \pm 0.3)\% \text{ (Babar)}$$

$$Q = (29.0 \pm 0.1)\% \text{ (Belle)}$$

$$Q = \epsilon(1 - 2w)^2$$

ϵ : efficiency

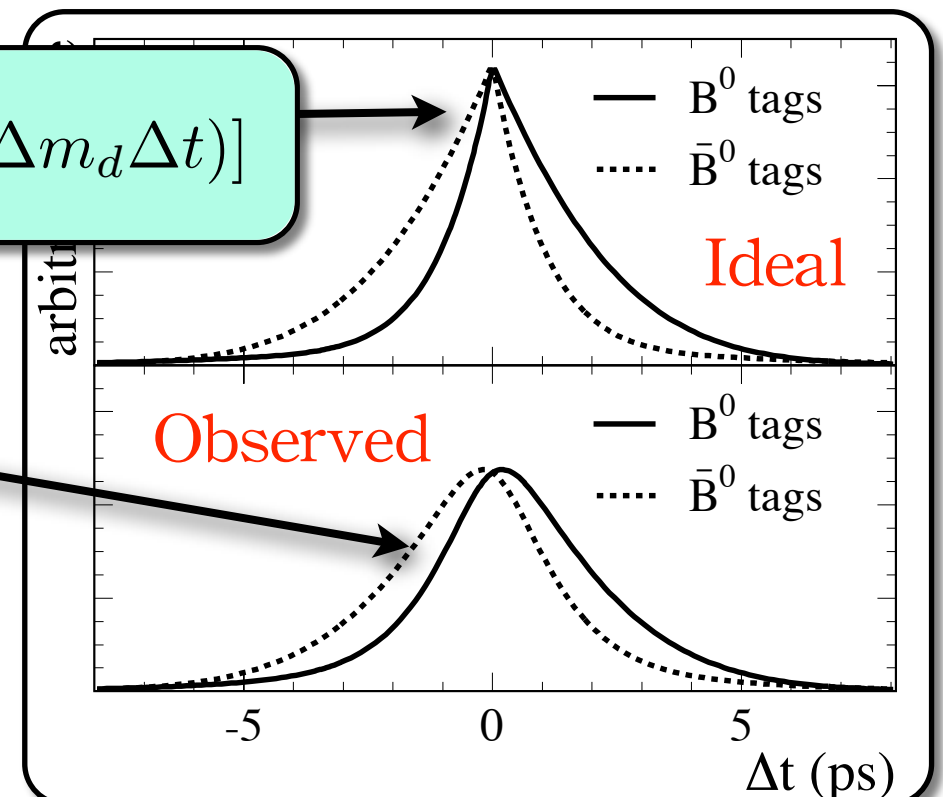
w : mistag rate

- Δt and flavor tag (\pm) go into decay rate:

$$f_{\pm}(\Delta t) = \frac{e^{-|\Delta t|/\tau}}{4\tau} [1 \pm (-\eta_f S_f \sin(\Delta m_d \Delta t) - C_f \cos(\Delta m_d \Delta t))]$$

- Modify $f_{\pm}(\Delta t)$ for experimental Δt resolution and tagging performance.

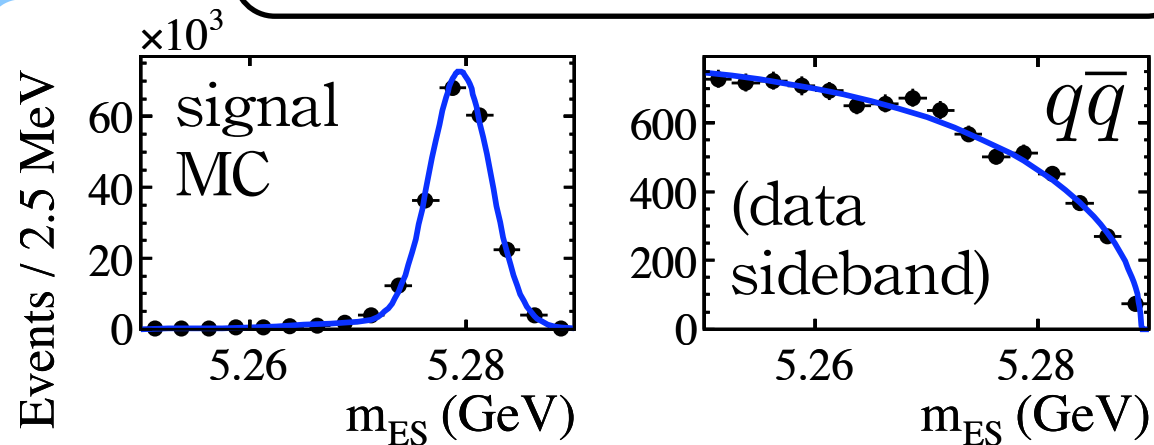
- Parameters of $f_{\pm}(\Delta t)$ obtained from a large sample of fully reconstructed self-tagging B decays.



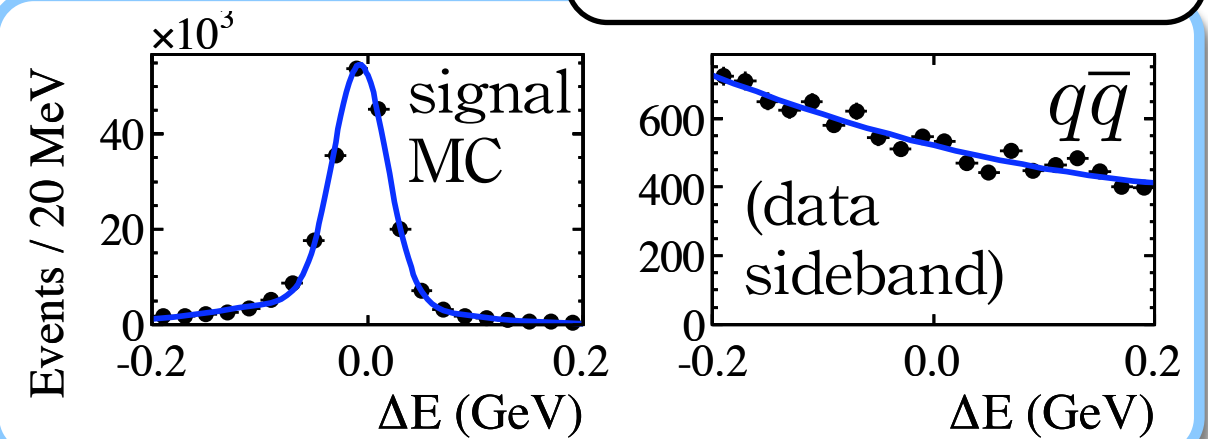
Maximum Likelihood Fit

- Components for signal, $e^+e^- \rightarrow q\bar{q}$ ($q = u, d, s, c$), charmed and charmless $B\bar{B}$ decays.
- Discriminate with variables related to B meson kinematics:

$$m_{\text{ES}} \equiv M_{bc} \equiv \sqrt{E_{\text{beam}}^2 - \mathbf{p}_B^{*2}}$$

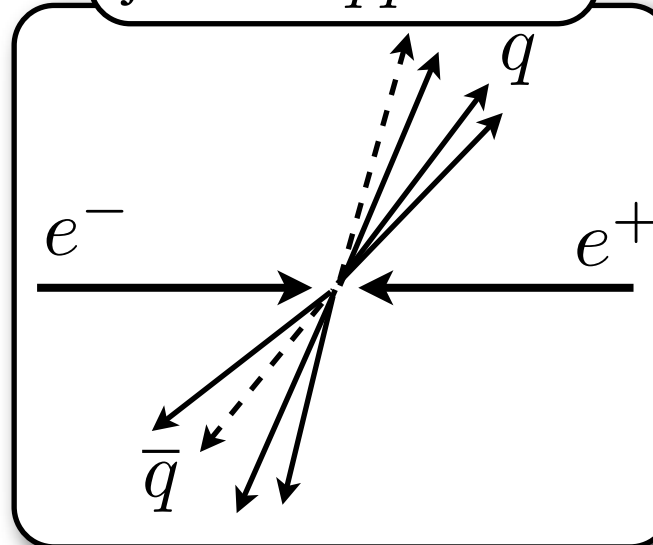


$$\Delta E \equiv E_B^* - E_{\text{beam}}$$

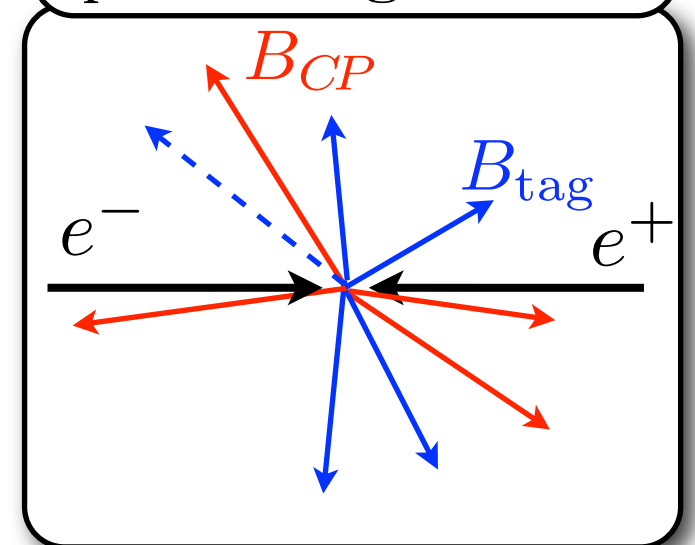


- Variables that exploit differing event topologies:
 - Babar's Fisher discriminant (\mathcal{F}).
 - Belle's likelihood ratio ($\mathcal{R}_{s/b}$).

jet-like $q\bar{q}$ event

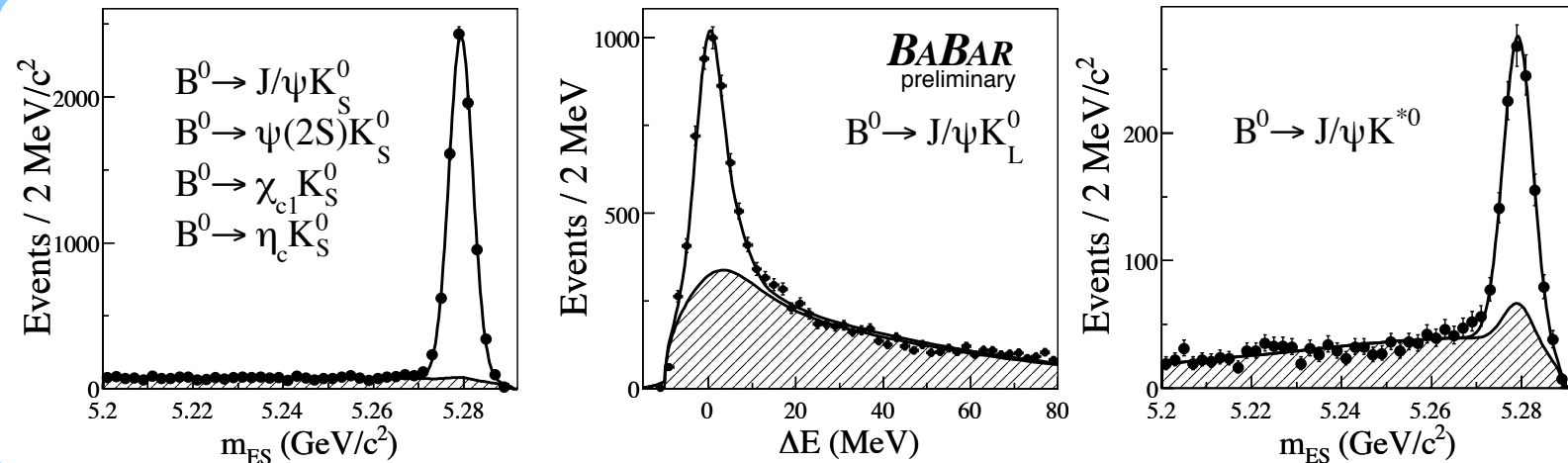
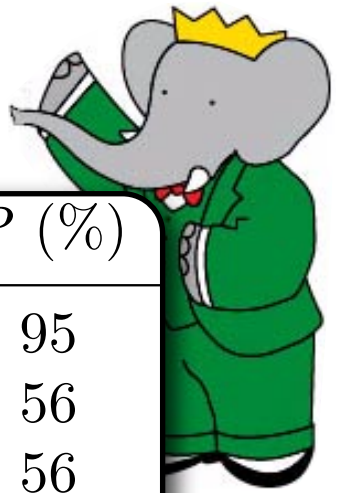


spherical signal event

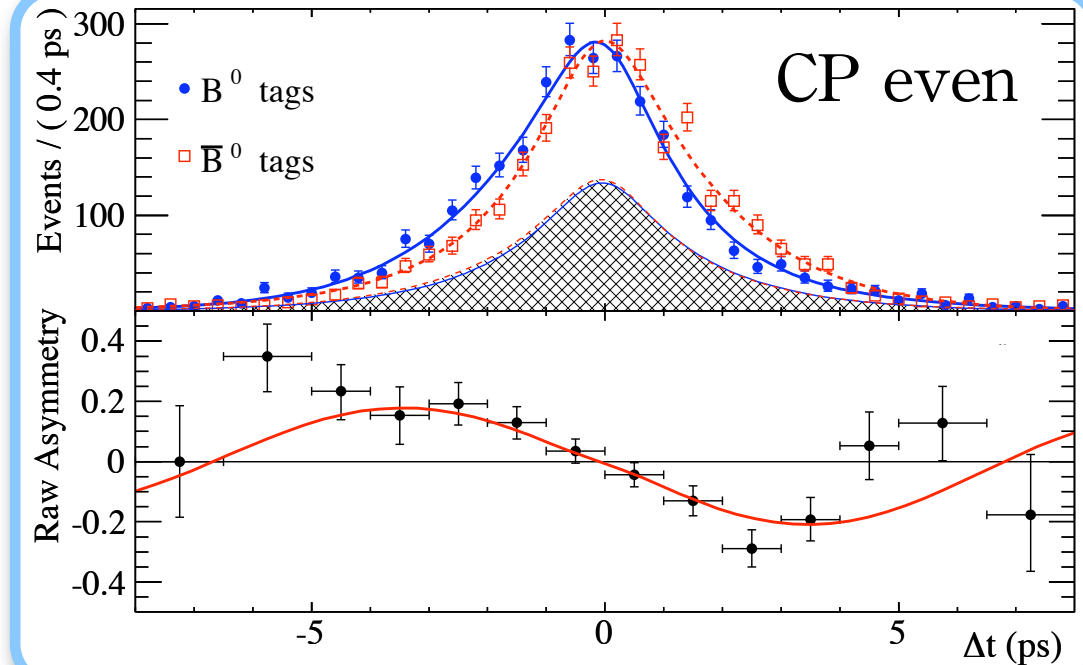
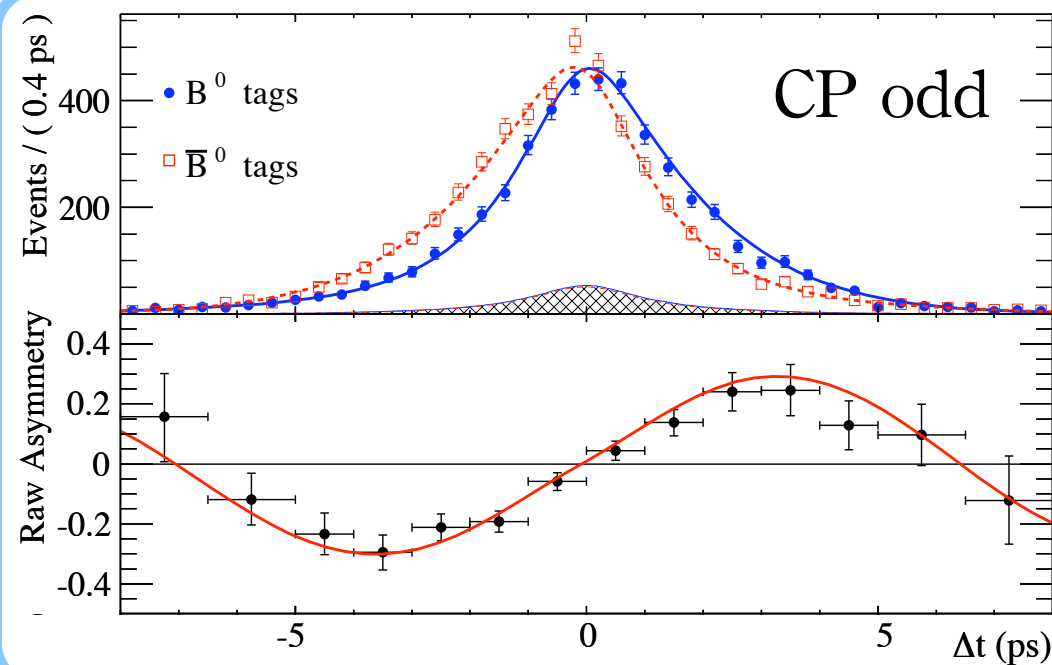


$b \rightarrow c\bar{c}s$ modes

arXiv:0808.1903 (2008), 465M $B\bar{B}$
(accepted by PRD)



Mode	N_{evts}	P (%)
$J/\psi K_S^0$	9073	95
$J/\psi K_L^0$	7813	56
$J/\psi K_0^{*0}$	1735	56
$\psi(2S) K_S^0$	1157	87
$\chi_{c1} K_S^0$	517	88
$\eta_c K_S^0$	512	79
Total	20807	76



$$S = 0.691 \pm 0.029 \pm 0.014$$

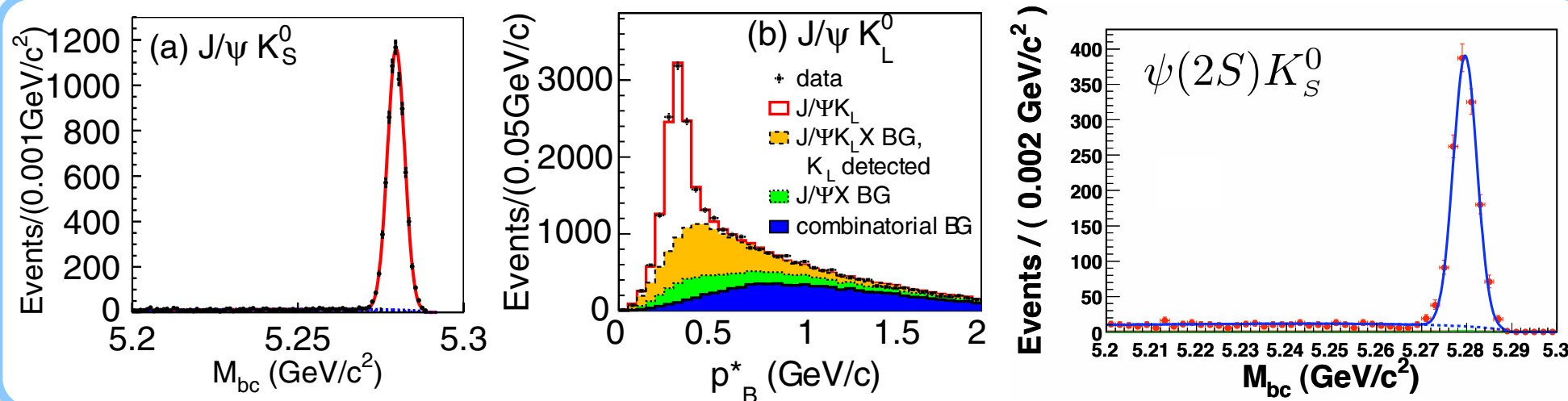
$$C = 0.027 \pm 0.020 \pm 0.016$$

Dominant systematic:

- S: Δt resolution model.
- C: Interference in tag-side DCSD.

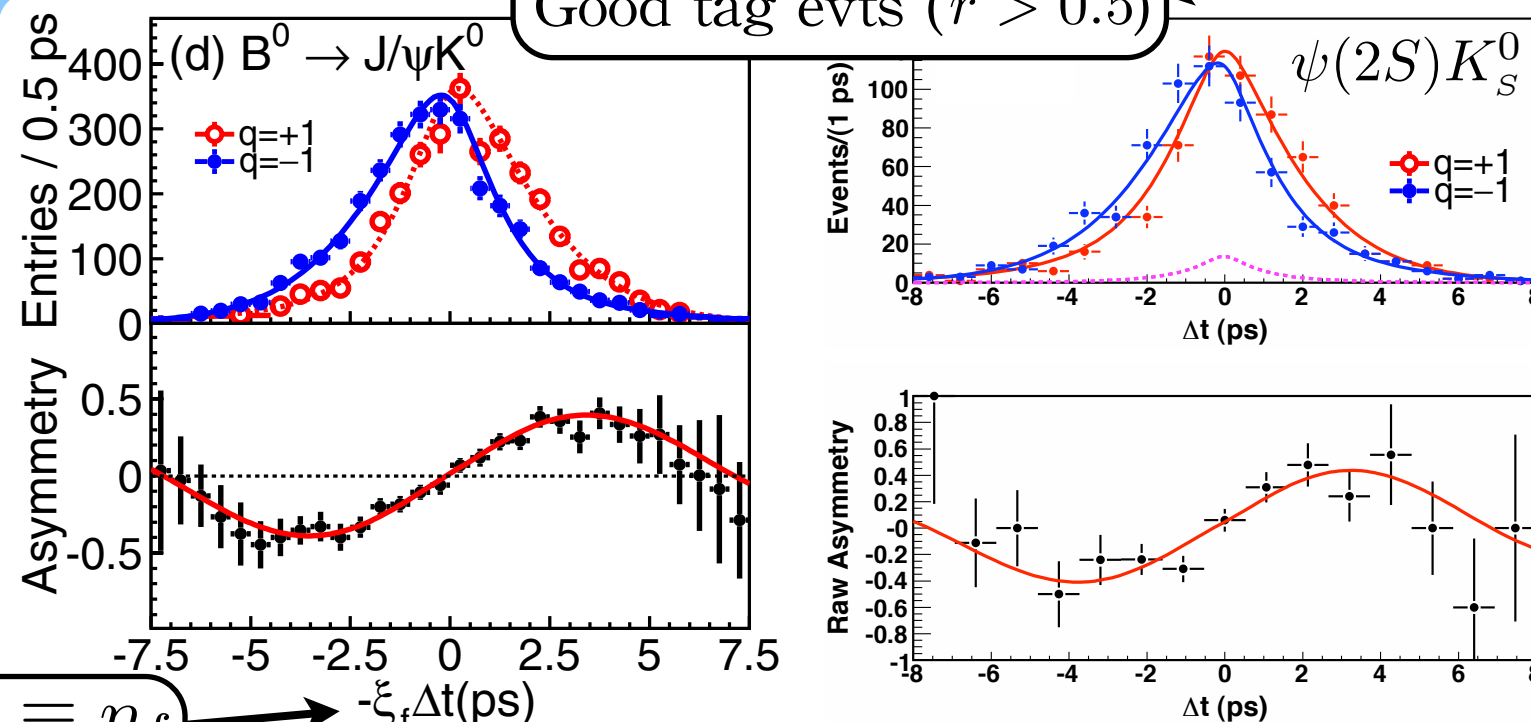
$b \rightarrow c\bar{c}s$ modes

PRL 98 031802 (2007), 535M $B\bar{B}$



Good tag evts ($r > 0.5$)

r is output of tagging algo.



$\xi_f \equiv \eta_f$

$$S = 0.642 \pm 0.031 \pm 0.017$$

$$C = 0.018 \pm 0.021 \pm 0.014$$

$$S = 0.720 \pm 0.090 \pm 0.030$$

$$C = 0.040 \pm 0.070 \pm 0.050$$

Mode	N_{evts}	P (%)
$J/\psi K_S^0$	7484	—
$J/\psi K_L^0$	6512	—
$\psi(2S) K_S^0$	1284	92

Dominant systematics:

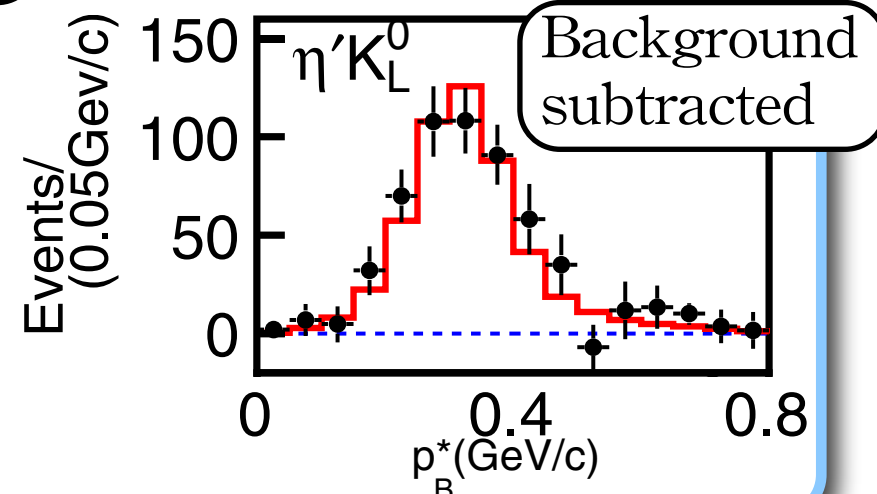
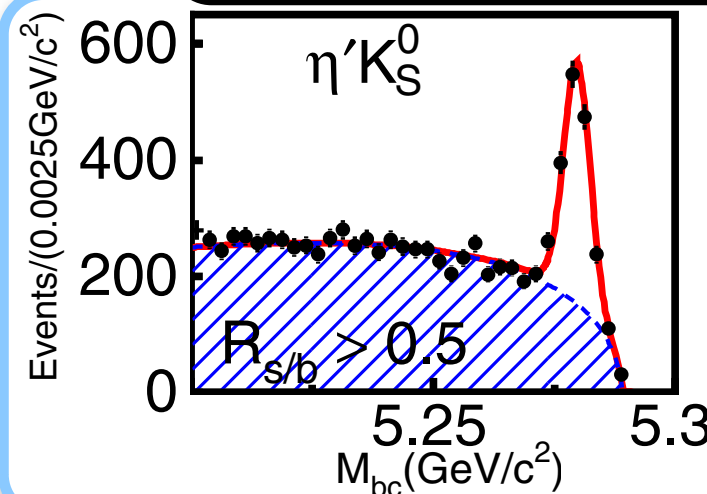
- S: vertex reconstruction.
- C: interference in tag-side DCSD.

$$B^0 \rightarrow \eta' K^0$$

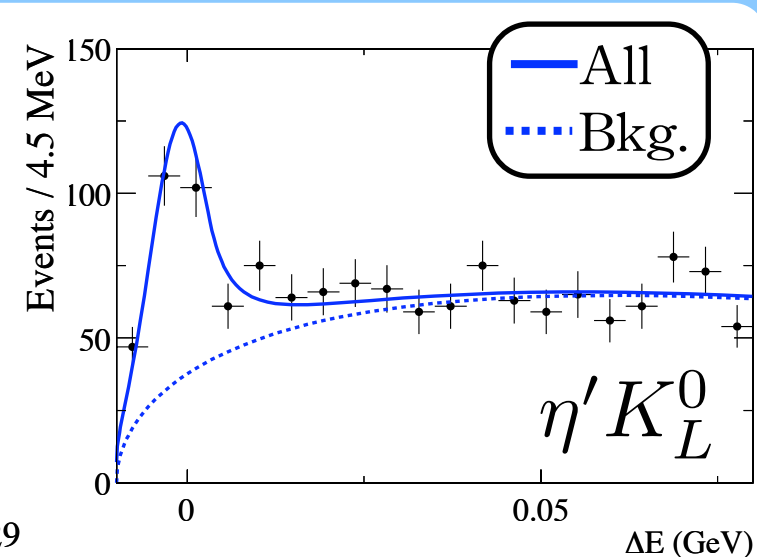
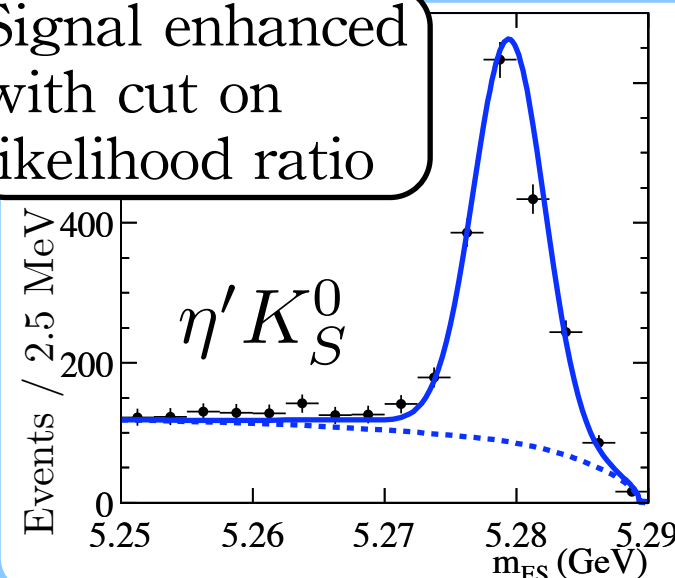
- Large BF (65×10^{-6}) yields small errors on S_f and C_f .
- 7 decay channels:
 $\eta'(\rho\gamma, \eta_{\gamma\gamma}\pi^+\pi^-, \eta_{3\pi}\pi^+\pi^-) K_S(\pi^+\pi^-)$
 $\eta'(\rho\gamma, \eta_{\gamma\gamma}\pi^+\pi^-) K_S(\pi^0\pi^0)$
 $\eta'(\eta_{\gamma\gamma}\pi^+\pi^-, \eta_{3\pi}\pi^+\pi^-) K_L$

Mode	Event yields	
	Belle	BABAR
$\eta' K_S^0$	1421 ± 46	1959 ± 58
$\eta' K_L^0$	454 ± 39	556 ± 38

Signal enhanced with cut on ΔE and $\mathcal{R}_{s/b}$



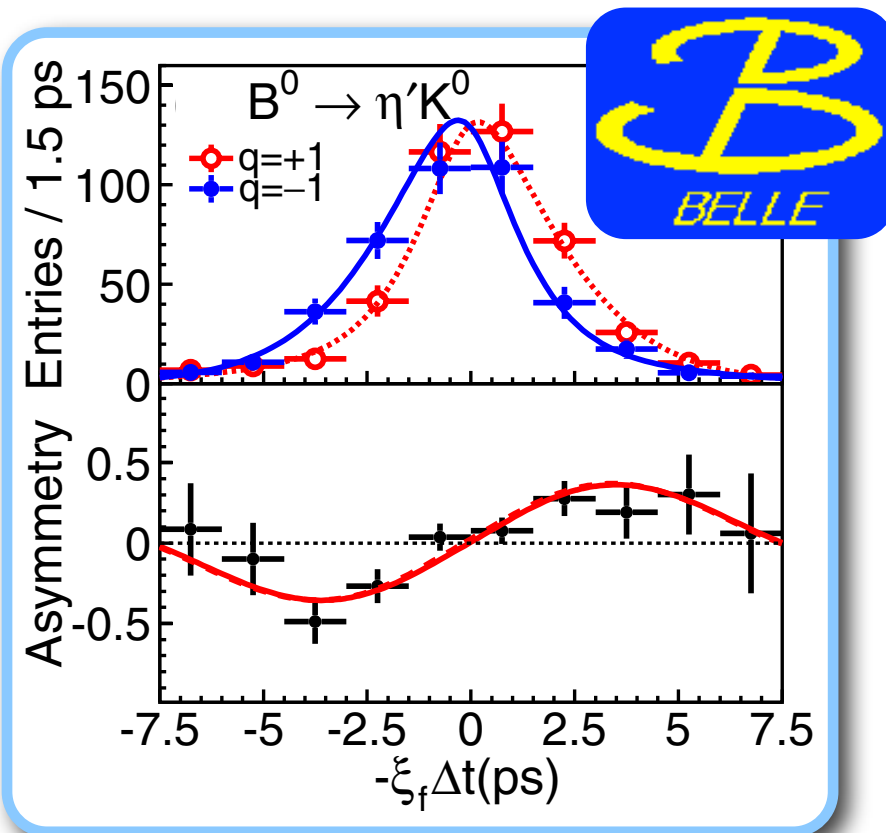
Signal enhanced with cut on likelihood ratio



$$B^0 \rightarrow \eta' K^0$$

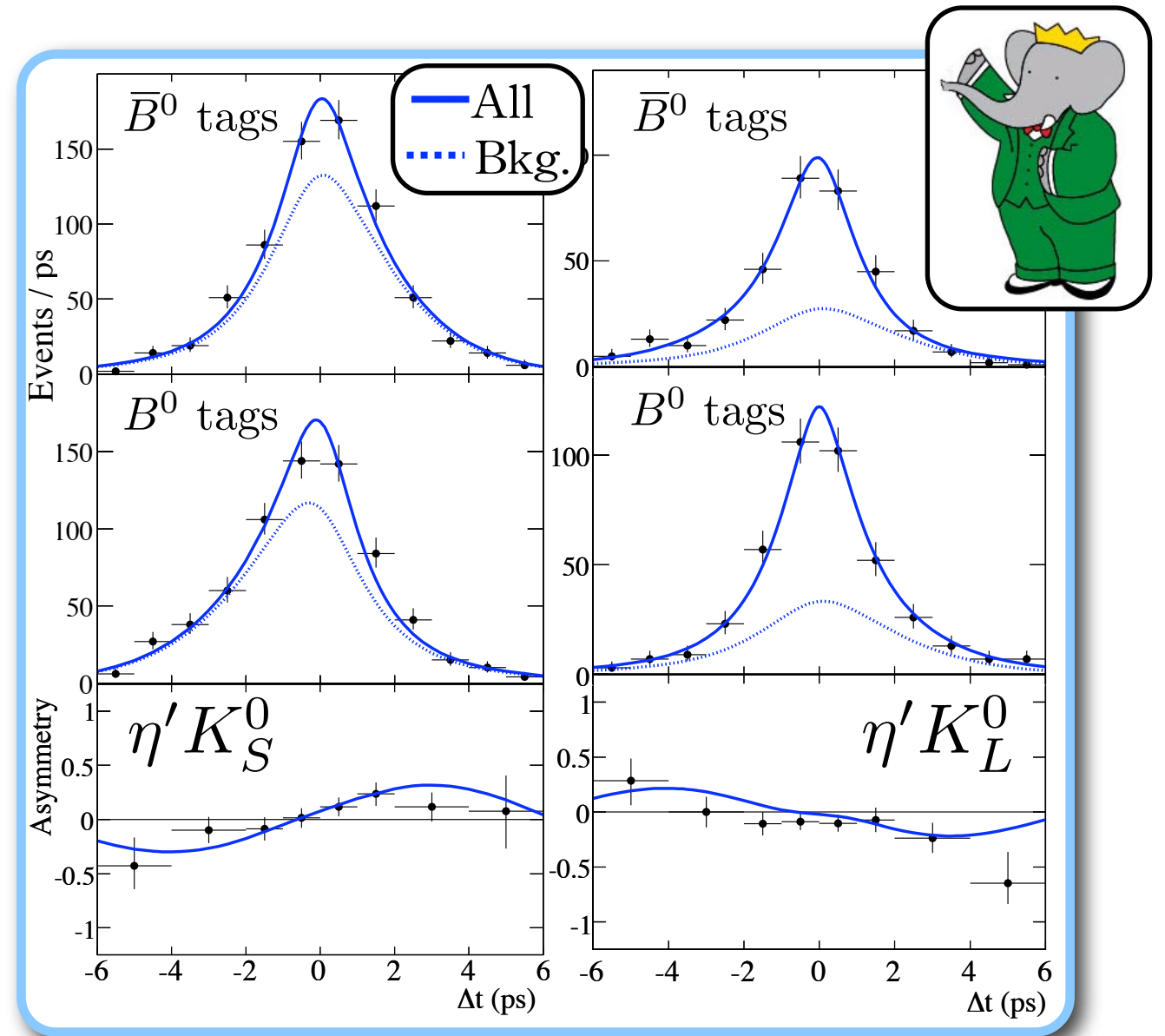
BABAR : PRD 79 052003 (2009)

Belle : PRL 98 031802 (2007)



Dominant systematic for both:

- S: Δt resolution model.
- C: Interference in tag-side DCSD.



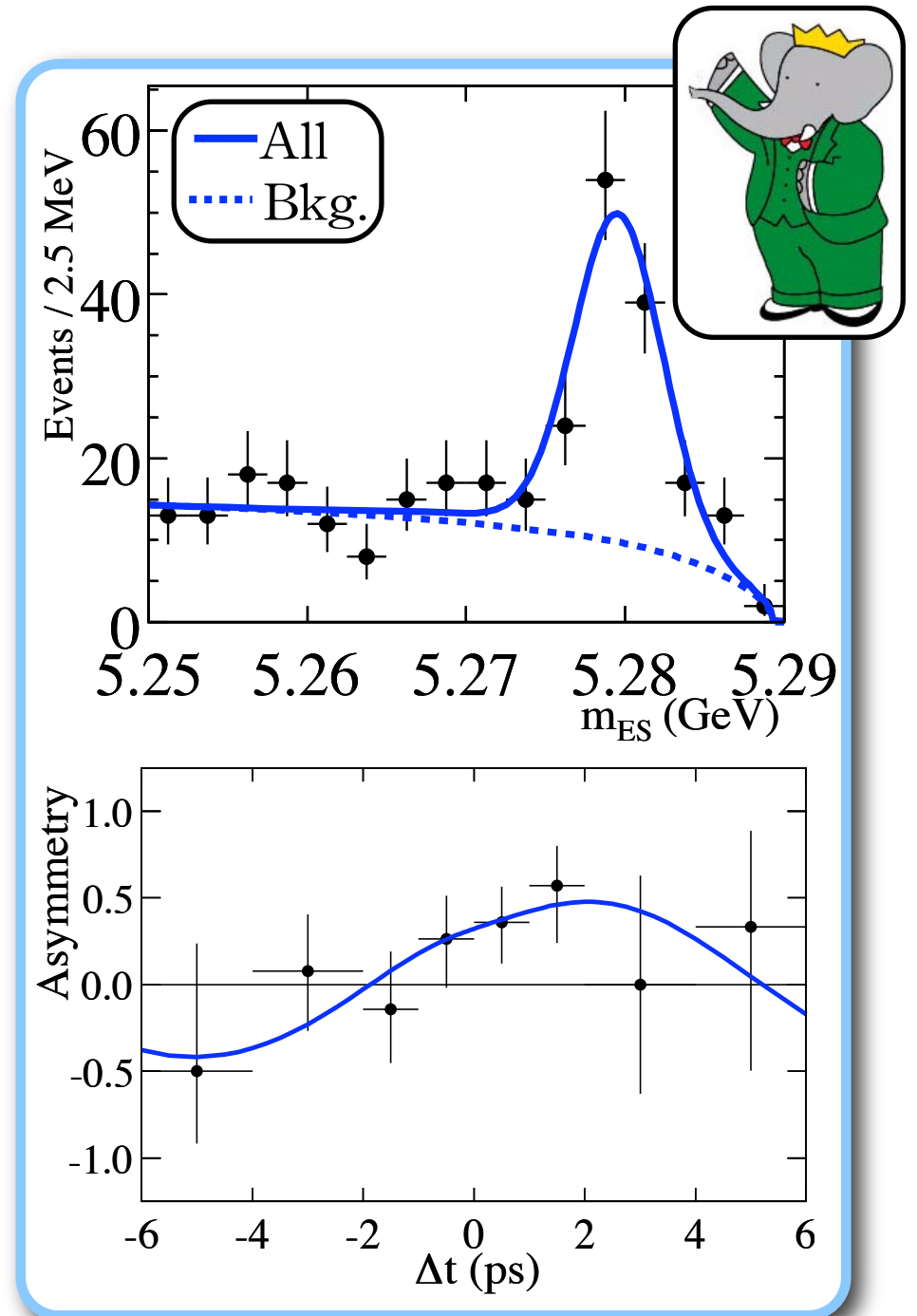
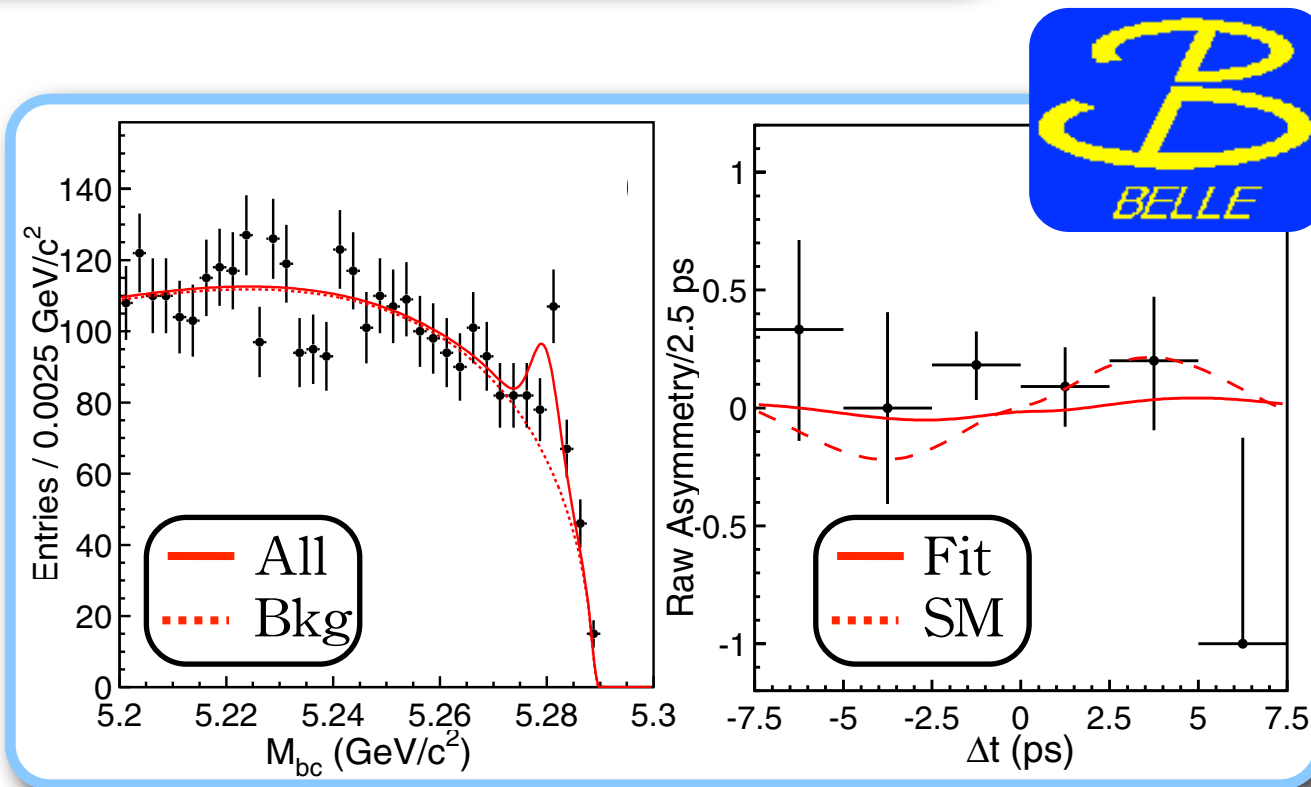
Mode	Belle	<i>BABAR</i>
$-\eta S_{\eta' K_S^0}$	0.67 ± 0.11	$0.53 \pm 0.08 \pm 0.02$
$C_{\eta' K_S^0}$	0.03 ± 0.07	$-0.11 \pm 0.06 \pm 0.02$
$-\eta S_{\eta' K_L^0}$	0.46 ± 0.24	$0.82 \pm 0.19 \pm 0.02$
$C_{\eta' K_L^0}$	-0.09 ± 0.16	$0.09 \pm 0.14 \pm 0.02$
$S_{\eta' K^0}$	$0.64 \pm 0.10 \pm 0.04$	$0.57 \pm 0.08 \pm 0.02$
$C_{\eta' K^0}$	$0.01 \pm 0.07 \pm 0.05$	$-0.08 \pm 0.06 \pm 0.02$

$$B^0 \rightarrow \omega K_S^0$$

BABAR : PRD 79 052003 (2009), 465M $B\bar{B}$
Belle : PRD 76 091103 (2007), 535M $B\bar{B}$

- Branching fraction $\sim 6 \times 10^{-6}$.
- Belle uses ω mass.
- Babar uses ω mass and helicity.
- Reconstruct:

$$\omega \rightarrow \pi^+ \pi^- \pi^0, K_S^0 \rightarrow \pi^+ \pi^-$$

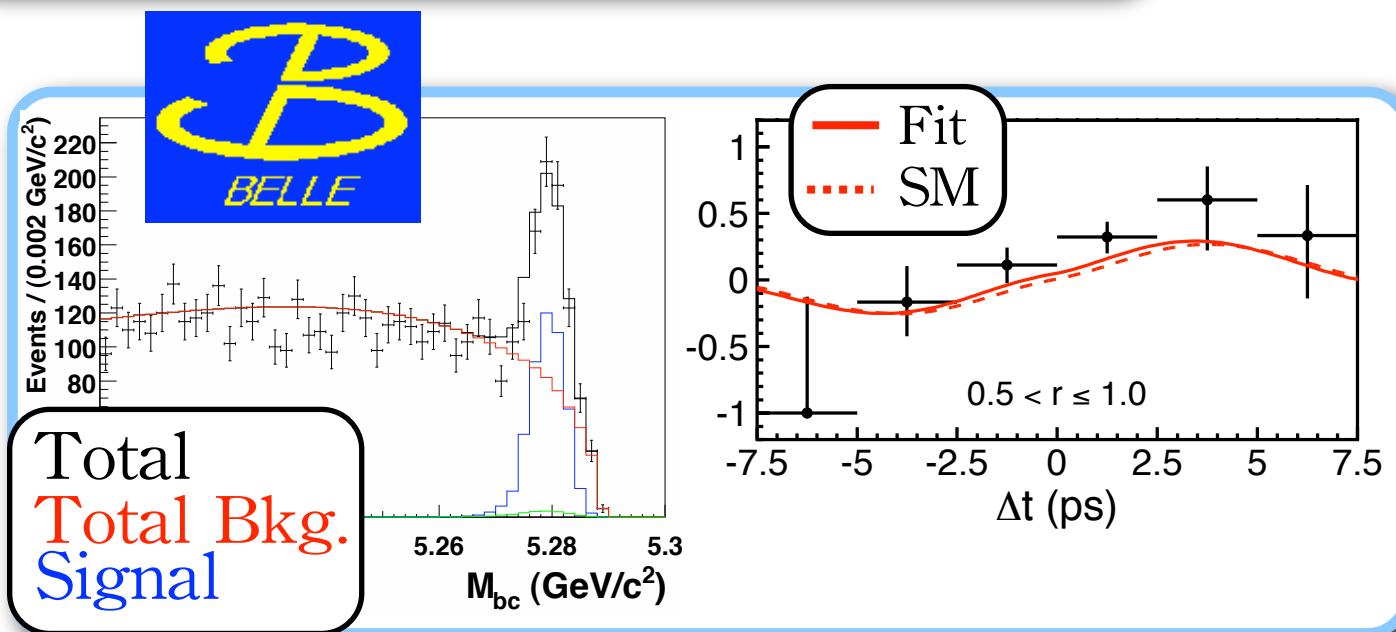


	Belle	<i>BABAR</i>
N_{evts}	118 ± 18	163 ± 18
$S_{\omega K_S^0}$	$0.11 \pm 0.46 \pm 0.07$	$0.55^{+0.26}_{-0.29} \pm 0.02$
$C_{\omega K_S^0}$	$0.09 \pm 0.29 \pm 0.06$	$-0.52^{+0.22}_{-0.20} \pm 0.03$

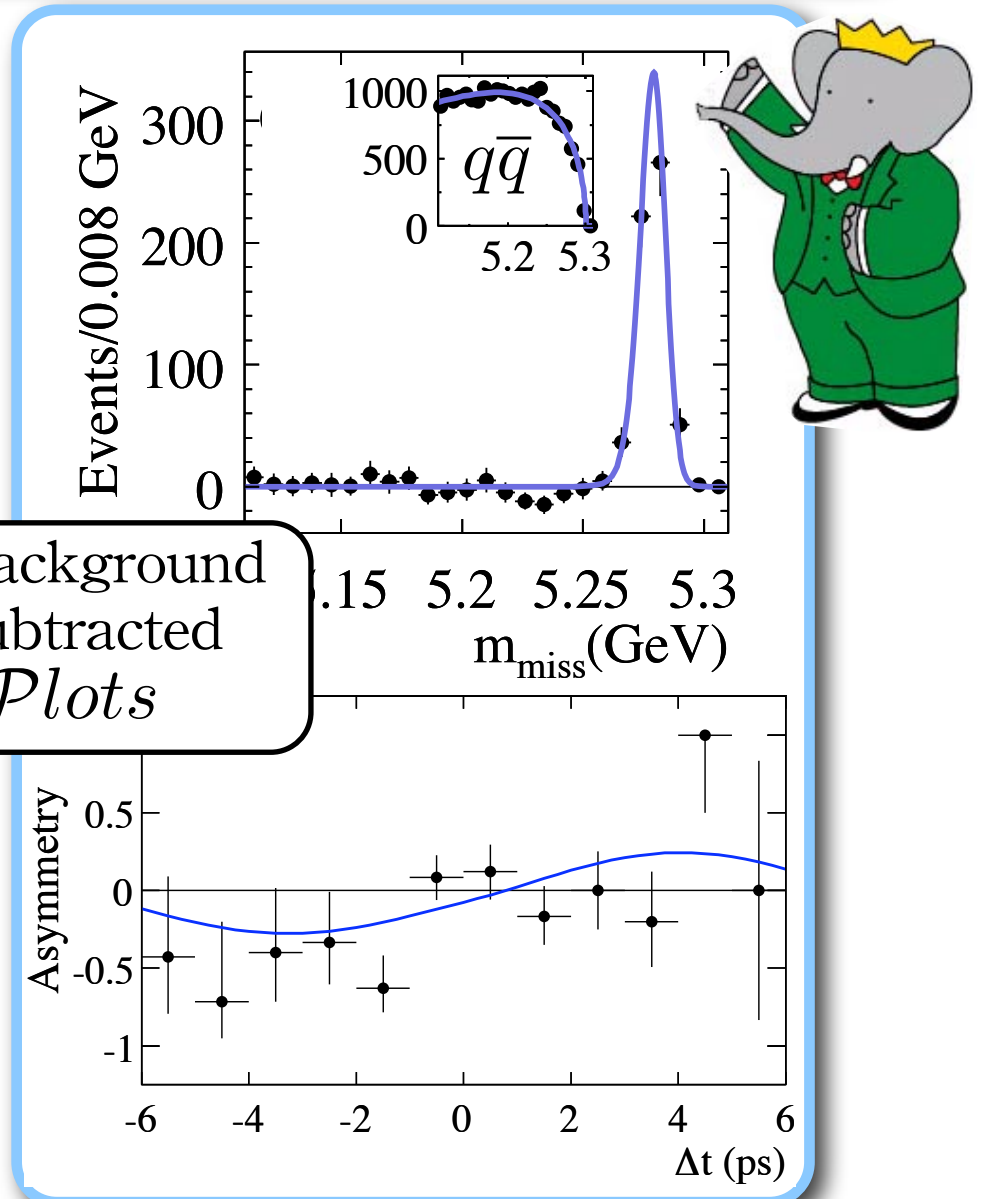
$$B^0 \rightarrow \pi^0 K_S^0$$

BABAR : PRD 79 052003 (2009), 465 M $B\bar{B}$
Belle : 0809.4366 (2008), 657 M $B\bar{B}$

- No tracks from B decay vertex!
- 60% of signal B candidates make hits in inner silicon tracker.
- Obtain Δt in these events with constraints on average interaction point (and B lifetime for Babar).



Background
subtracted
*s*Plots



	Belle	<i>BABAR</i>
$N_{\pi^0 K_S^0}$	657 ± 37	556 ± 32
$N_{\pi^0 K_L^0}$	285 ± 52	—
S	$0.67 \pm 0.31 \pm 0.08$	$0.55 \pm 0.20 \pm 0.03$
C	$0.14 \pm 0.13 \pm 0.06$	$0.13 \pm 0.13 \pm 0.03$

- All events constrain C.
- Belle also uses $\pi^0 K_L^0$ events to constrain C.

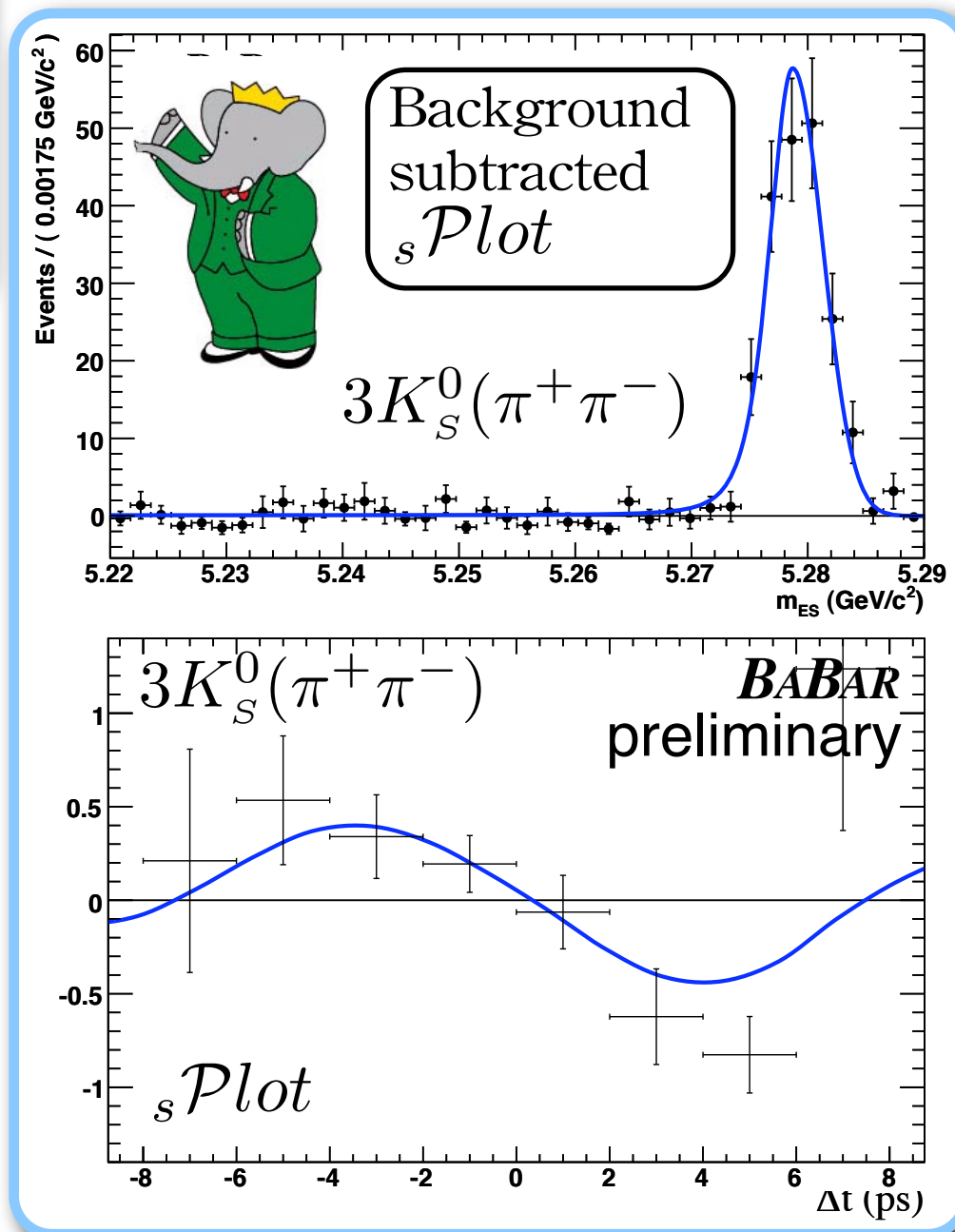
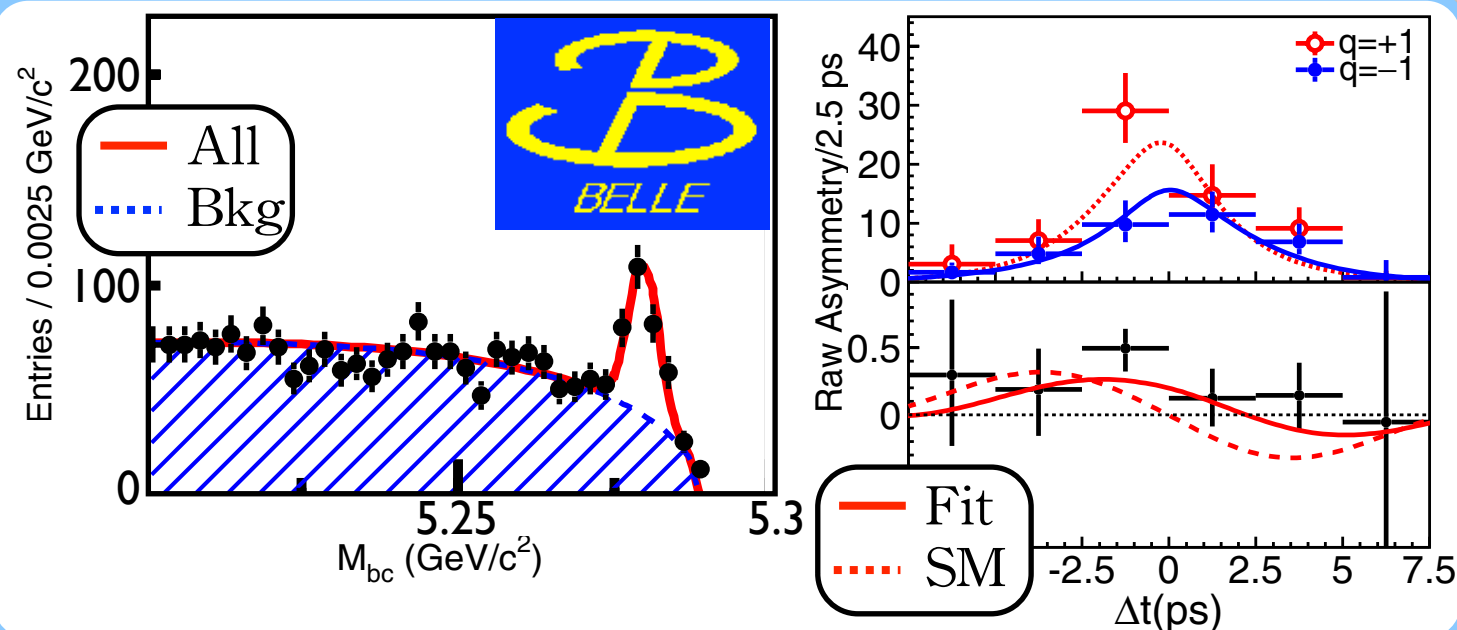
$$B^0 \rightarrow K_S^0 K_S^0 K_S^0$$

BABAR : CKM 2008 preliminary, 465M $B\bar{B}$
Belle : PRL 98 031802 (2007), 535M $B\bar{B}$

- Reconstruct:

$$2K_S^0(\pi^+\pi^-)K_S^0(\pi^0\pi^0) \text{ and } 3K_S^0(\pi^+\pi^-)$$

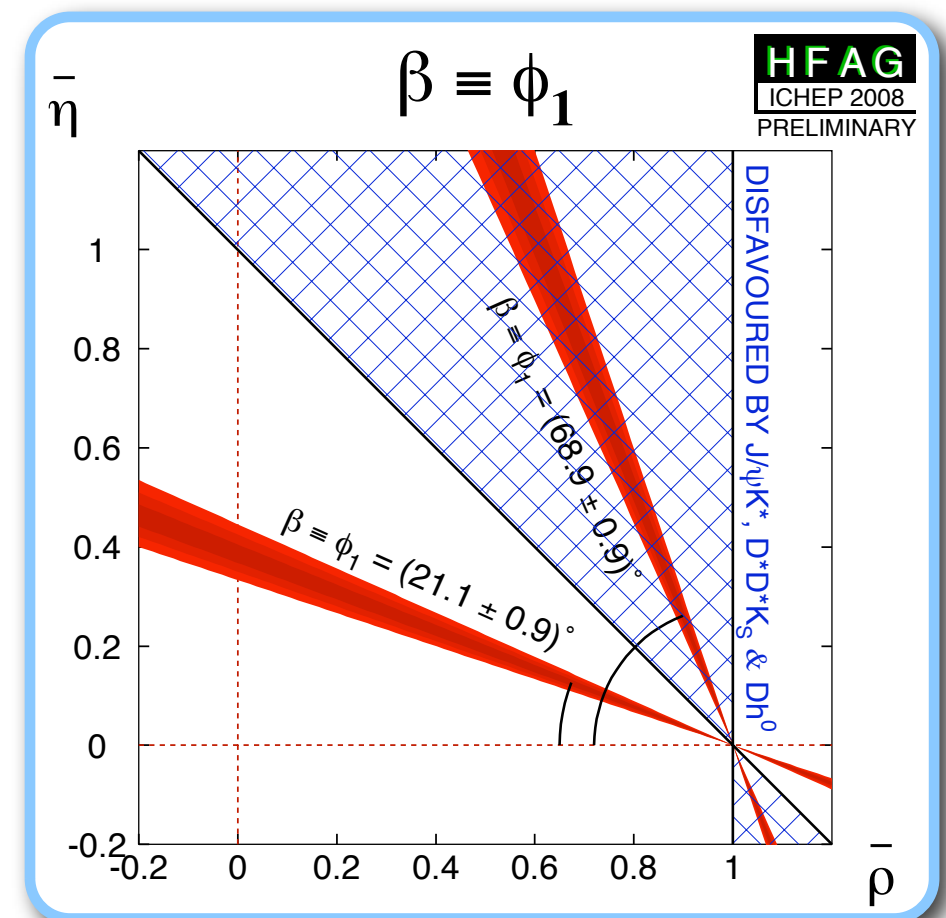
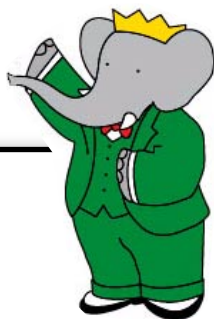
- Again, no tracks from B decay vertex.
- Require one K_S^0 to make hits in inner tracker.
- Constrain average interaction point and B lifetime.

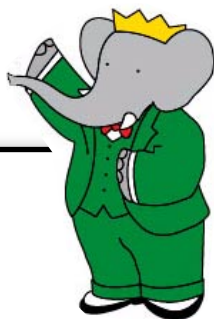



	Belle	<i>BABAR</i>
N_{tag}	185 ± 17	274 ± 21
$-\eta S$	$0.30 \pm 0.32 \pm 0.08$	$0.90^{+0.20}_{-0.18} {}^{+0.04}_{-0.03}$
C	$-0.31 \pm 0.20 \pm 0.07$	$-0.16 \pm 0.17 \pm 0.03$

$\frac{\pi}{2} - \beta$ Ambiguity

- Interference between CP-even and -odd amplitudes makes $J/\psi K^{*0}, D^{(*)} D^{(*)} K_S^0$ sensitive to $\cos 2\beta$.
- Interference in $D^{(*)}$ Dalitz plot makes $D^{(*)} h^0$ sensitive to $\cos 2\beta$.
- Interference in DP makes $K^+ K^- K_S^0$ sensitive to β .



Final State	 $\cos 2\beta$	C.L. for $\cos 2\beta > 0$	 $\cos 2\beta$	C.L. for $\cos 2\beta > 0$
$D^{(*)} + D^{(*)} - K_S^0$	$0.38 \pm 0.24 \pm 0.05^{[1]}$	94%	$-0.23^{+0.43}_{-0.41} \pm 0.13^{[2]}$	—
$D^{(*)} h^0$	$0.42 \pm 0.49 \pm 0.16^{[3]}$	86%	$1.87^{+0.40}_{-0.53} \pm 0.22^{[4]}$	98.3%
$J/\psi K^{*0}$	$3.32^{+0.76}_{-0.96} \pm 0.27^{[5]}$	89%	$0.56 \pm 0.79 \pm 0.11^{[6]}$	—
$K^+ K^- K_S^0$	$\beta = (29.5 \pm 4.5 \pm 1.5)^\circ [7]$	4.8 σ	$\beta_{\phi K_S^0} = (21.2^{+9.8}_{-10.4} \pm 2.0)^\circ [8]$	—

[1] PRD 74 091101 (2006) (230M BB)

[2] PRD 76 072004 (2007) (449M BB)

[3] PRL 99 231802 (2007) (383M BB)

[4] PRL 97 081801 (2006) (386M BB)

[5] PRD 71 032005 (2005) (88M BB)

[6] PRL 95 091601 (2005) (275M BB)

[7] arXiv:0808.0700 (2008) (465M BB)

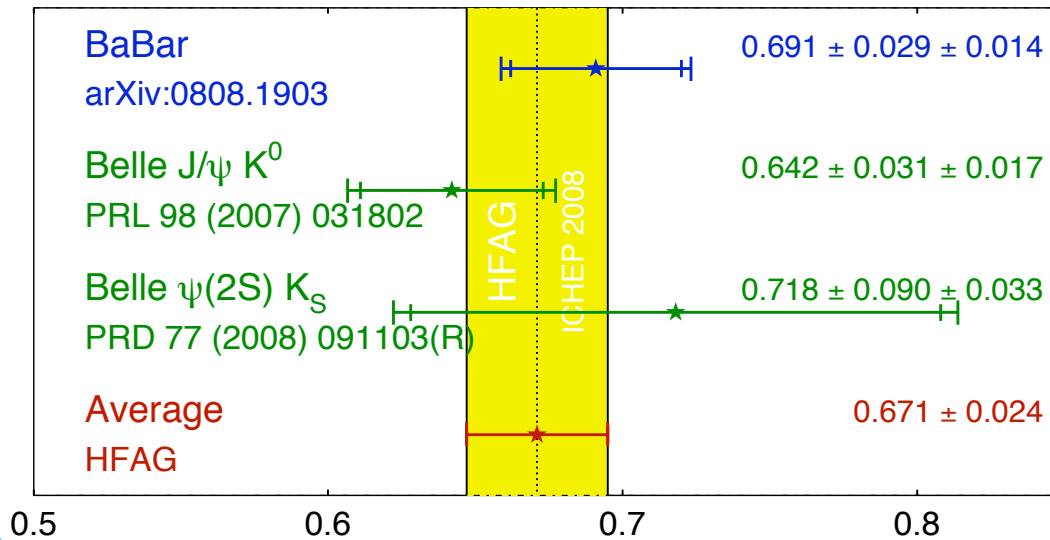
[8] ICHEP08 preliminary (657M BB)

Summary

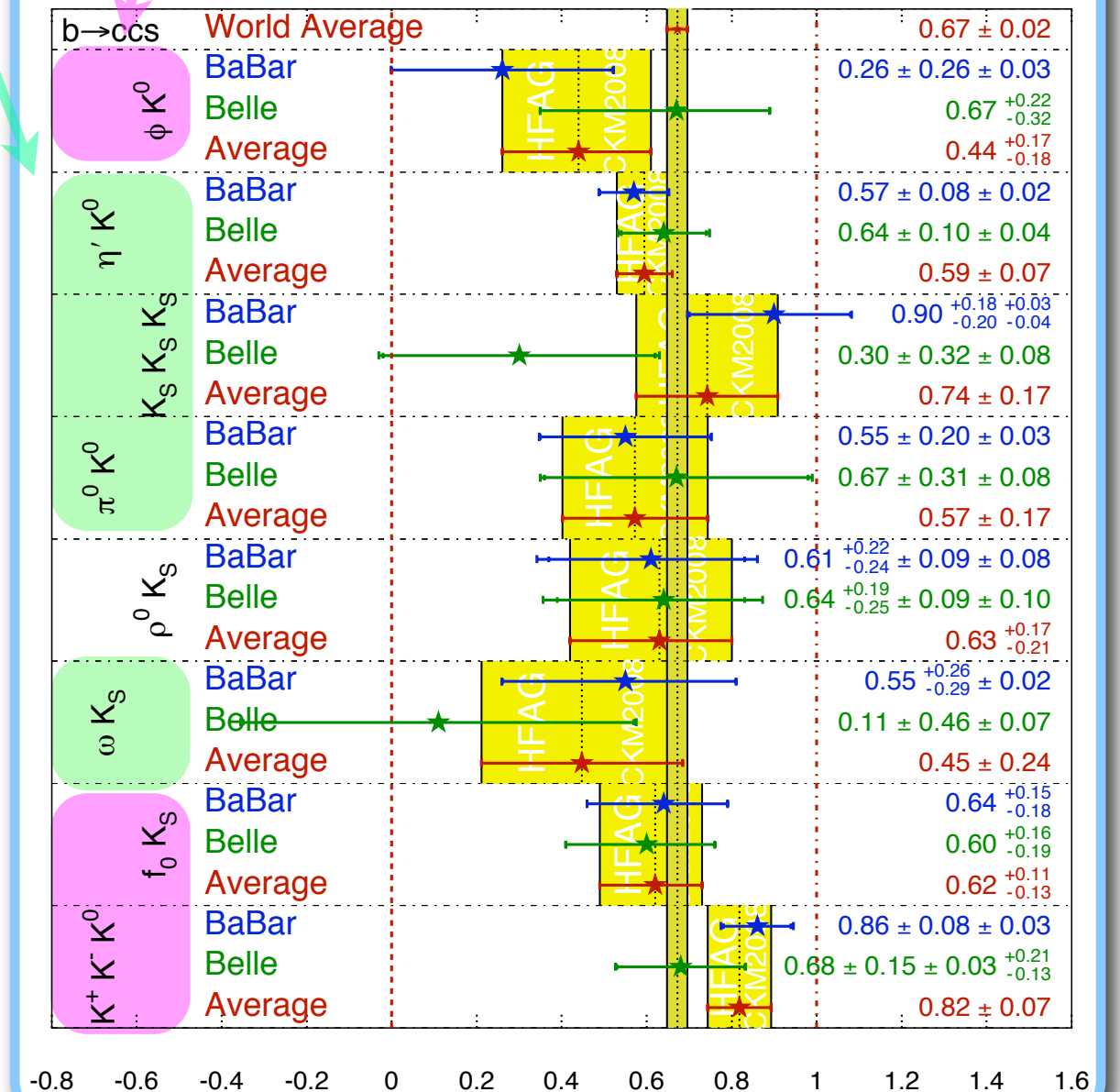
This talk

“CPV at B factories, $B \rightarrow K\pi$, $b \rightarrow s\gamma$ ”
Yu Nakahama (Heavy Flav. & CKM-3)

$$\sin(2\beta) \equiv \sin(2\phi_1) \quad \text{HFAG} \quad \text{ICHEP 2008} \quad \text{PRELIMINARY}$$



$$\sin(2\beta^{\text{eff}}) \equiv \sin(2\phi_1^{\text{eff}}) \quad \text{HFAG} \quad \text{CKM2008} \quad \text{PRELIMINARY}$$



- New physics is not dominant.
- At LHC: Difficult to trigger on ϕK^0 ; impossible to trigger on $\eta' K^0$
- At Super Flavor Factories:
 - Measurements of β_{eff} and β systematics limited.
 - Experimental/theoretical uncertainties comparable.

Babar systematics on $\sin 2\beta$ from $J/\psi K^0$

Source/sample		Full	$J/\psi K^0$	$J/\psi K_S^0$	$J/\psi K_L^0$
Beamspot	S_f	0.0013	0.0021	0.0027	0.0000
	C_f	0.0006	0.0010	0.0021	0.0001
Mistag differences	S_f	0.0077	0.0057	0.0059	0.0083
	C_f	0.0047	0.0069	0.0053	0.0052
Δt resolution	S_f	0.0067	0.0068	0.0069	0.0071
	C_f	0.0027	0.0029	0.0034	0.0070
$J/\psi K_L^0$ background	S_f	0.0057	0.0063	0.0000	0.0271
	C_f	0.0007	0.0008	0.0000	0.0036
Background fraction and CP content	S_f	0.0046	0.0034	0.0036	0.0044
	C_f	0.0029	0.0021	0.0009	0.0107
m_{ES} parameterization	S_f	0.0022	0.0020	0.0026	0.0006
	C_f	0.0004	0.0005	0.0008	0.0002
$\Delta m_d, \tau_B, \Delta\Gamma_d/\Gamma_d$	S_f	0.0030	0.0033	0.0036	0.0040
	C_f	0.0013	0.0012	0.0011	0.0013
Tag-side interference	S_f	0.0014	0.0014	0.0014	0.0014
	C_f	0.0143	0.0143	0.0143	0.0143
Fit bias (MC statistics)	S_f	0.0023	0.0044	0.0041	0.0063
	C_f	0.0026	0.0044	0.0041	0.0060
Total	S_f	0.0135	0.0131	0.0119	0.0311
	C_f	0.0164	0.0187	0.0167	0.0270